

SIXTH SEMESTER B.Sc. DEGREE EXAMINATION, APRIL 2025**COMPUTER SCIENCE AND MATHEMATICS (DOUBLE MAIN)****GDMA6B10T: NUMERICAL ANALYSIS****Time: 2 Hours****Maximum: 60 Marks****SECTION A: Answer the following questions. Each carries two marks.****(Ceiling 20 marks)**

1. What is the remainder term or bound for the error involved in approximating a function $f(x)$ by an interpolating polynomial $P(x)$.
2. What is the difference equation associated with Euler's method?
3. Define forward difference and backward difference.
4. Express $\nabla^2 f_3$ in terms of the values of the function.
5. Write the conditions for applying Bisection algorithm to find a root for $f(x) = 0$ on the interval $[a, b]$.
6. Determine the linear Lagrange interpolating polynomial that passes through the points (2, 4) and (5, 1).
7. Write Second derivative midpoint Formula to approximate $f''(x)$ at x_0 .
8. Write Simpson's three-eighths rule for approximating $\int_a^b f(x) dx$.
9. Find h when approximating $\int_0^2 \frac{1}{1+x} dx$ using Trapezoidal rule.
10. Give an example of a Lipschitz function $f(t, y)$.
11. Define Numerical quadrature.
12. Write number of iteration necessary to approximate $y(1.2)$ from the IVP.
 $y' = y - t^2 + 1, 0 \leq t \leq 2, y(0) = 0.5$ $h = 0.2$ using Runge Kutta method of order 4.

SECTION B: Answer the following questions. Each carries five marks.**(Ceiling 30 marks)**

13. Use Stirling's formula to approximate $f(0.43)$ for the following data:

x	:	0.0	0.2	0.4	0.6	0.8
f(x)	:	1.00000	1.22140	1.49182	1.82212	2.22554

14. Compare the Trapezoidal rule when approximating $\int_0^2 x^2 dx$.

(PTO)

15. Using Runge-Kutta method of order four to find w_1 for the following initial-value problem: $y' = \cos 2t + \sin 3t$, $0 \leq t \leq 1$, $y(0) = 1$, with $h = 0.5$.
16. Use a fixed-point iteration method to determine a solution accurate to within 10^{-4} for $x = \tan x$, for x in $[4, 5]$.
17. Show that there is a unique solution to the initial-value problem $y' = 1 + t \sin(ty)$, $0 \leq t \leq 2$, $y(0) = 0$.
18. For the given function $f(x) = \tan x$, let $x_0 = 0$, $x_1 = 0.6$. Construct interpolation polynomial of degree one to approximate $f(0.45)$, and find the absolute error.
19. Use Euler's method to approximate the solution for the following initial-value problem: $y' = 1 + (t - y)^2$, $2 \leq t \leq 3$, $y(2) = 1$, with $h = 0.5$

SECTION C: Answer any *one* question. The question carries *ten* marks.

20. The equation $x^2 - 10 \cos x = 0$ has two solutions, ± 1.3793646 . Use Newton's method to approximate the solution to within 10^{-5} with $p_0 = -100$.
21. Approximate $\int_0^2 \frac{1}{1+x} dx$ using:
 - a. Trapezoidal rule and find absolute error.
 - b. Simpson's rule and find absolute error.

(1 x 10 = 10 Marks)