(PAGES 2)

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Name:

THIRD SEMESTER B.Sc. DEGREE EXAMINATION, NOVEMBER 2023 (Supplementary – 2018 Admission) STATISTICS COMPLEMENTARY COURSE TO MATHEMATICS AND C.S ASTA3C03T: STATISTICAL INFERENCE

Time: 3 Hours

Maximum Marks: 80

PART A: Answer all the questions. Each carries one mark.

- 1. Define Statistic.
- 2. Write the pdf of a chi-square distribution.
- 3. State the relation connecting t and F statistics.
- 4. Define F statistic
- 5. Write all four desirable properties of a good estimator.
- 6. State the Neyman factorization theorem.
- 7. State the concept of a 95% confidence interval.
- 8. Write exact confidence intervals for difference of proportions.
- 9. Define hypothesis.
- 10. Write assumptions of one sample t test.
- 11. Define the term attribute.
- 12. Comment on critical region.

(12 x 1 = 12 Marks)

PART B: Answer all the questions. Each carries two marks.

- 13. Distinguish between Standard error and Standard deviation.
- 14. Write any four applications of t statistics.
- 15. Examine the differences between type I and II errors.
- 16. Distinguish between point estimation and interval estimation.
- 17. Write any two confidence interval using t distribution.
- 18. Distinguish between simple and composite hypotheses.
- 19. Write the test statistic for large sample tests concerning mean equality of means.
- 20. Distinguish between significance and power of a test.
- 21. Write for tests based on Chi-square distribution.

PART C: Answer any *five* questions. Each carries *six* marks.

- 22. Derive F distribution from two independent Chi-square distributions.
- 23. Let $X \sim N(n, p)$. Find an unbiased estimator for n, and p based on sample of size m.
- 24. Derive Chi-square distribution from Normal distribution.
- 25. Explain Method of maximum likelihood and method of moments.
- 26. Derive the 95% confidence interval for mean difference.
- 27. Wrtie a short note on small sample tests based on t distribution for equality of means.
- 28. Derive the 95% confidence interval for variances using F statistic.
- 29. Explain the working procedure of Chi-square for goodness of fit.

 $(5 \times 6 = 30 \text{ Marks})$

PART D: Answer any two questions. Each carries ten marks.

- 30. Write the interrelationship between Chi-square, t and F statistic.
- 31. Explain four desirable properties of a good estimator using proper examples.
- 32. A study is conducted to analyze the effectiveness of two different teaching methods, A and B, in improving students' test scores. The scores of 15 students who underwent method A and 15 students who underwent method B are given below. Perform a test to determine if there is a significant difference between the two teaching methods.

| Observation | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
|-------------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| No. | | | | | | | | | | | | | | | |
| Method A | 80 | 78 | 67 | 74 | 83 | 69 | 78 | 74 | 89 | 86 | 77 | 73 | 80 | 71 | 85 |
| Method B | 72 | 70 | 69 | 71 | 69 | 70 | 71 | 72 | 70 | 70 | 70 | 70 | 69 | 70 | 71 |

(2 x 10 = 20 Marks)