D2BST2301

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Name:

SECOND SEMESTER B.Sc. DEGREE EXAMINATION, APRIL 2024

(Regular/Improvement/Supplementary)

STATISTICS: COMPLEMENTARY COURSE FOR MATHEMATICS & CS GSTA2C02T: PROBABILITY THEORY

Time: 2 Hours

Maximum Marks: 60

SECTION A: Answer the following questions. Each carries two marks.

(Ceiling 20 Marks)

- 1. What is sample space? A coin is tossed until a head appears, write down the sample space.
- 2. State empirical definition of probability.
- 3. A problem is given to two students and their chances of solving it are 1/2 and 1/3 respectively. What is the probability that the problem will be solved?
- 4. A can hit a target four times in 5 shots, B, three times in 4 shots, C two times in 3 shots.

 Calculate the probability that only one will hit the target.
- 5. Let X be a random variable with p.d.f $f(x) = kx^2(1-x)$; 0 < x < 1. Find the value of k.
- 6. If X has the pdf $f(x) = \begin{cases} 1, & 0 \le x \le 1 \\ 0, & otherweise \end{cases}$

Obtain the distribution of - 2logX.

7. If
$$f(x) = \frac{1}{2^x}$$
, $x = 1, 2, 3, ...$

Show that $E(2^X)$ does not exists.

- 8. What are the properties of moment generating function?
- What do you mean by conditional probability function.
- 10. For any two random variables X and Y, show that E(E(X|Y)) = E(X).
- 11. If X is a random variable with pdf f(x), Prove that $E(X^2) \ge [E(X)]^2$.
- 12. What are the properties of distribution function?

SECTION B: Answer the following questions. Each carries five marks.

(Ceiling 30 Marks)

- 13. Twenty-five books are placed at random in a shelf. Find the probability that a particular pair of books shall be:
 - (i) Always together.
- (ii) Never together.
- 14. State and prove addition theorem on probability for two events.

- 15. Find p.d.f of a random variable with distribution function $F(x) = 1 e^{-x}$, x > 0.
- 16. Define raw moments and central moments. Obtain the relation between raw moments and central moments.
- 17. Two dice are thrown. X represents the sum of the two numbers that come up. Determine E(X) and V(X).
- 18. Find the mean of $Y = X^2 + 1$ if X has probability function.

x :	0	1	2	3
P(x):	0.1	0.2	0.3	0.4

19. Find the m.g.f for $f(x) = \frac{1}{8}(1+x), 2 < x < 4$.

SECTION C: Answer any one question. Each carries ten marks.

- 20. (a) State and prove Bayes' theorem.
 - (b) The probabilities of X, Y and Z becoming managers are 4/9, 2/9 and 1/3 respectively. The probabilities that the Bonus Scheme will be introduced if X, Y and Z becomes managers are 3/10, 1/2 and 4/5 respectively.
 - (i) What is the probability that Bonus Scheme will be introduced?
 - (ii) If the Bonus Scheme has been introduced, what is the probability that the manager appointed was X?
- 21. The p.d.f of two random variables (X, Y) is given by $f(x, y) = \begin{cases} 2, & 0 < x < y < 1 \\ 0, & elsewhere. \end{cases}$

Find the marginal distributions. Also find the conditional mean and variance of X given Y = y.

 $(1 \times 10 = 10 \text{ Marks})$