

FIRST SEMESTER FYUGP EXAMINATION NOVEMBER 2024
MINOR
MAT1MN101 CALCULUS

Time : 2 Hrs

Maximum Marks : 70

BL - Bloom's Taxonomy Level (1 to 6)

CO - Course Outcome

Section A		Ceiling Marks : 24		
Answer all questions. Each carries 3 marks.				
No.	Question	M	BL	CO
1.	Find the slope and equation of the tangent line to the graph of the equation $y = -x^2 + 4x$ at the point $P(2, 4)$.	3	2	CO1
2.	Find the derivative of $f(x) = (2 + 3x^2)(x^3 - 5)$	3	4	CO1
3.	Find the differential of the function $f(x) = \sqrt{2x^2 + 1}$ at $x = 2$	3	1	CO1
4.	Find the critical numbers of the function $f(x) = x - 3x^{\frac{1}{3}}$	3	3	CO1 CO2
5.	Define Inflection points of a function.	3	2	CO1 CO2
6.	Define Differential of a Function	3	2	CO1
7.	Find $\int \frac{dx}{(2x-4)^3}$	3	4	CO3
8.	Evaluate $\sum_{k=1}^{10} k^2$	3	3	CO3
9.	Expand $\sum_{k=1}^{n-1} \sin\left(\frac{k\pi}{n}\right)$	3	5	CO3
10.	Define arc length function	3	1	CO3
Section B		Ceiling Marks : 36		
Answer all questions. Each question carries 6 marks.				
No.	Question	M	BL	CO
11.	a) State Quotient Rule of Differentiation b) Find the derivative of $f(x) = \frac{2x^2+x}{x^3-1}$	6	3	CO1
12.	At a distance of 12000 ft from the launch site, a spectator is observing a rocket being launched vertically. What is the speed of the rocket at the instant when the distance of the rocket from the spectator is 13,000 ft and increasing at the rate of 480 ft/sec?	6	4	CO1
13.	Water is poured to a conical funnel at the rate of 1 in ³ /sec and flows out at the rate of $\frac{1}{2}$ in ³ /sec. The funnel is a right circular cone with height of 4 in. and a radius of 2 in. at the base. How fast is the water level changing when the water is 2 in. high?	6	6	CO1
14.	The edge of a cube was measured and found to be 3 in. with maximum possible error of 0.02 in. Find the approximate maximum percentage error that would be incurred in computing the volume of the cube using this measurement.	6	5	CO1
15.	a) Find the intervals where the function $f(x) = x^2 - 2x$ is increasing and decreasing b) Find the relative maximum and relative minimum of this function	6	3	CO1 CO2
16.	Evaluate $\sum_{k=1}^{10} (3k^2)(2k + 1)$	6	3	CO3
17.	Find the area of the region bounded by the graphs of $x = y^2$ and $y = x - 2$ by integrating with respect to y axis	6	4	CO3
18.	Find the area bounded by the regions $x = y^2, x = 2y + 3$	6	6	CO3
Section C				
Answer any 1 question. Each carries 10 marks. (1x10=10 marks)				
No.	Question	M	BL	CO
19.	Sketch the graph of the function $f(x) = x^3 - 3x^2 + 1$	10	6	CO1 CO2

20.	<p>a) Find the area of the surface obtained by revolving the graph of $x = y^3$ on the interval $[0,1]$ about the y- axis</p> <p>b) Find the area of the surface obtained by revolving the graph of $f(x) = \sqrt{x}$ on the interval $[0,2]$ about the x- axis</p>	10	2	CO3
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